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Proposed Syllabus  
for B.Sc.  
Mathematics  
paper for 6  
semesters under  
Choice Based  
Credit Scheme  
(CBCS)

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Effective from the academic  
year 2014-2015

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Department of Mathematics  
Bangalore University

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7. Plotting of standard Polar curves using Scilab/Maxima.
8. Plotting of standard parametric curves using Scilab/Maxima.
9. Scilab/Maxima programs for area and volume.
10. Solution of Differential equation using Scilab/Maxima and plotting the solution-I.
11. Solution of Differential equation using Scilab/Maxima and plotting the solution-II.
12. Solution of Differential equation using Scilab/Maxima and plotting the solution-III.
13. Solution of Differential equation using Scilab/Maxima and plotting the solution-IV.

**Note:** The above list may be changed annually with the approval of the BOS in UG (Mathematics).

### **THIRD SEMESTER MATHEMATICS-III**

**(4 lecture hours per week+ 3 hours of practicals /week per batch of not more than 10 students)**

**(56 HOURS)**

#### **THEORY**

#### **1. ALGEBRA - III**

##### **Groups**

Order of an element of a group – properties related to order of an element- subgroup generated by an element of a group –coset decomposition of a group, Cyclic groups-properties- modulo relation- index of a group –Lagrange’s theorem- consequences.

(14 lecture hours)

#### **2. ANALYSIS – I**

##### **a) Sequences Of Real Numbers**

Definition of a sequences-Bounded sequences- limit of a sequences-convergent, divergent and oscillatory sequences- Monotonic sequences and their properties- Cauchy’s criterion.

##### **b) Series Of Real Numbers**

Definition of convergence, divergence and oscillation of series -properties of Convergence series - properties of series of positive terms – Geometric series Tests for convergence of series -p- series - comparison of series Cauchy’s root Test -D Alembert’s test. Raabe’s test ,- Absolute and conditional convergence-D’ Alembert test for absolute convergence - Alternating series - Leibnitz test.

Summation of binomial, exponential and logarithmic series.(28 lecture hours)

### 3. CALCULUS - III

#### Differential Calculus

Recapitulation of Equivalence Class and partition of a set. Definition of the limit of a function in  $\epsilon$ - $\delta$  form –continuity- types of discontinuities. Properties of continuous function on a closed interval ( boundedness, attainment of bounds and taking every value between bounds). Differentiability -Differentiability implies Continuity – Converse not true. Rolle’s Theorem- Lagrange’s and Cauchy’s First Mean Value Theorem (Lagrange’s form ) - Maclaurin’s expansion. Evaluation of limits by L’ Hospital’s rule (14 lecture hours)

#### Suggested distribution of lecture hours

1. Algebra – III (Groups): 1 hour / week.
2. Analysis-I (sequences of real numbers and series of real numbers):2 hours /week
3. Calculus - III(differential calculus): 1 hour / week.

#### Text Books/open source materials

1. Herstein I N, *Topics in Algebra*, 4th ed. New Delhi, India: Vikas Publishing House Pvt. Ltd, 1991.
2. Boumslag and Chandler, *Schaum’s outline series on groups*, 2010.
3. S.C.Malik and Savita Arora, *Mathematical Analysis*, 2nd ed. New Delhi, India: New Age international (P) Ltd., 1992
4. Shanthi Narayan and P K Mittal, *Differential Calculus*, Reprint. New Delhi: SChand and Co. Pvt. Ltd., 2014.
5. [www.scilab.org](http://www.scilab.org).
6. [wxmaxima.sourceforge.net](http://wxmaxima.sourceforge.net)
7. [www.geogebra.org](http://www.geogebra.org)

#### Reference Books

1. Michael Artin, *Algebra*, 2nd ed. New Delhi, India: PHI Learning Pvt. Ltd., 2011.
2. Vashista, *A First Course in Modern Algebra*, 11th ed.: Krishna Prakasan Mandir, 1980.
3. John B Fraleigh, *A First course in Abstract Algebra*, 3rd ed.: Narosa Publishing House., 1990.
4. R Balakrishan and N.Ramabadran, *A Textbook of Modern Algebra*, 1st ed. New Delhi, India: Vikas publishing house pvt. Ltd., 1991.
5. Richard R Goldberg, *Methods of Real Analysis*, Indian ed. New Delhi, India: Oxford and IBH Publishing Co., 1970.

6. G B Thomas and R L Finney, *Calculus and analytical geometry*, Addison Wesley, 1995.
7. J Edwards, *An elementary treatise on the differential calculus: with applications and numerous examples*, Reprint. Charleston, USA: BiblioBazaar, 2010.
8. N P Bali, *Differential Calculus*, New ed. New Delhi, India: Laxmi Publications (P) Ltd., 2010.
9. S Narayanan & T. K. Manicavachogam Pillay, *Calculus*: S. Viswanathan Pvt. Ltd., vol. I & II 1996.
10. Frank Ayres and Elliott Mendelson, *Schaum's Outline of Calculus*, 5th ed. USA: Mc. Graw Hill., 2008.
11. E Spiegel, *Schaum's Outline of Advanced Calculus*, 5th ed. USA: Mc. Graw Hill., 2009.

### Useful web links:

1. <http://www.themathpage.com/>
2. <http://www.abstractmath.org/>
3. <http://ocw.mit.edu/courses/mathematics/>
4. <http://www.math.unl.edu/~webnotes/contents/chapters.htm>
5. <http://www-groups.mcs.st-andrews.ac.uk/~john/analysis/index.html>
6. <http://web01.shu.edu/projects/reals/index.html>
7. <http://www.mathcs.org/analysis/reals/index.html>
8. <http://planetmath.org/encyclopedia/TopicsOnCalculus.html>
9. <http://ocw.mit.edu/OcwWeb/Mathematics/18-01Fall-2005/CourseHome/index.htm>
10. <http://mathworld.wolfram.com/Calculus.html>
11. <http://ocw.mit.edu/courses/mathematics/>

## PRACTICALS –III

### Mathematics practicals with FOSS tools for computer programs ( 3 hours/ week per batch of not more than 10 students)

#### LIST OF PROBLEMS

1. Examples to verify Lagrange's theorem.
2. Examples for finding left and right coset and finding the index of a group.
3. Illustration of convergent, divergent and oscillatory sequences using Scilab/Maxima.
4. Illustration of convergent, divergent and oscillatory series using Scilab/Maxima.
5. Scilab/Maxima programs to find the sum of the series and its radius of convergence.
6. Using Cauchy's criterion to determine convergence of a sequence (simple examples).
7. Using Cauchy's criterion on the sequence of partial sums of the series to determine convergence of a series.

8. Testing the convergence of binomial, exponential and logarithmic series and finding the sum.
9. Scilab/Maxima programs to illustrate continuity of a function.
10. Scilab/Maxima programs to illustrate differentiability of a function and unequal left hand and right hand limits for discontinuous functions.
11. Scilab/Maxima programs to verify Rolle's theorem and Lagrange's theorem.
12. Scilab/Maxima programs to verify Cauchy's mean value theorem and finding Taylor's theorem for a given function.
13. Evaluation of limits by L'Hospital's rule using Scilab/Maxima.

**Note:** The above list may be changed annually with the approval of the BOS in UG (Mathematics). Geogebra/Octave may also be used in place of scilab/maxima.

## **FOURTH SEMESTER**

### **MATHEMATICS - IV**

**(4 lecture hours per week+ 3 hours of practicals /week per batch of not more than 10 students)**

**(56 HOURS)**

#### **THEORY**

#### **1. ALGEBRA –IV**

##### **Groups**

Normal subgroups-examples and problems –Quotient group-Homomorphism and Isomorphism of groups-Kernel and image of a homomorphism-Normality of the Kernel-Fundamental theorem of homomorphism- properties related to isomorphism-Permutation group-Cayley's theorem.

(14 lecture hours)

#### **2. ANALYSIS -II**

##### **Fourier Series**

Trigonometric Fourier series of functions with period  $2\pi$  and period  $2L$  – Half range Cosine and sine series.

(9 lecture hours)

#### **3. CALCULUS - IV**

##### **Differential Calculus**

Continuity and differentiability of a function of two and three variables – Taylor's Theorem and expansion of functions of two variables- Maxima and Minima of functions Of two variables. Method of Lagrange multipliers. (9 lecture hours)

#### **4. MATHEMATICAL METHODS - I**

Definition and basic properties Laplace transform of some common functions and Standard results –Laplace transform of periodic functions- Laplace transforms ,of derivatives And the integral of function- Laplace transforms, Heaviside function

convolution theorem (statement only) Inverse Laplace transforms.

(10 lecture hours)

## 5. DIFFERENTIAL EQUATIONS –II

Second and higher order ordinary linear differential equations with constant Coefficients- complementary function- particular integrals (standard types) Cauchy-Euler differential equation. Simultaneous linear differential equations (two variables) with constant coefficients. Solutions of second order ordinary linear differential equations with variable coefficients by the following methods.

- (i). When a part of complementary function is given
- (ii). Changing the independent variable
- (iii). Changing the dependent variable
- (iv). Variation of parameters
- (v). Conditions for exactness and the solution when the equation is exact.

(14 lecture hours)

### Suggested distribution of lecture hours

1. Algebra – IV (Rings ,Fields and Integral domains): 1 hour / week
2. Analysis – II (Fourier series), Calculus-IV (Differential Calculus) and Mathematical methods-I (Laplace transform): 2 hours / week.
3. Differential Equations II: 1 hour / week.

### Text Books/open source materials

1. Herstein I N, *Topics in Algebra*, 4th ed. New Delhi, India: Vikas Publishing House Pvt. Ltd, 1991.
2. Boumslag and Chandler, *Schaum's outline series on groups*, 2010.
3. Erwin Kreyszig, *Advanced Engineering Mathematics*, 8th ed. New Delhi, India: Wiley India Pvt. Ltd., 2010.
4. Shanthi Narayan and P K Mittal, *Differential Calculus*, Reprint. New Delhi: S Chand and Co. Pvt. Ltd., 2014.
5. M D Raisinghania, *Ordinary and Partial Differential Equations*, S Chand and Co. Pvt. Ltd., 2014.
6. [www.scilab.org](http://www.scilab.org).
7. [wxmaxima.sourceforge.net](http://wxmaxima.sourceforge.net)
8. [www.geogebra.org](http://www.geogebra.org)

### Reference Books

1. Michael Artin, *Algebra*, 2nd ed. New Delhi, India: PHI Learning Pvt. Ltd., 2011.

**PRACTICALS –IV**  
**Mathematics practicals with FOSS tools for computer programs**  
**(3 hours/ week per batch of not more than 10 students)**

**LIST OF PROBLEMS**

1. Illustrating homomorphism and isomorphism of groups.
2. Verification of Normality of a given subgroup.
3. Verifying Cayley's theorem and isomorphism theorems.
4. To plot periodic functions with period  $2\pi$  and  $2L$ .
5. To find full range trigonometric Fourier series of some simple functions with period  $2\pi$  and  $2L$ .
6. Plotting of functions in half-range and including their even and odd extensions.
7. To find the half-range sine and cosine series of simple functions.
8. Finding maxima/minima of functions of two variables.
9. Finding the Laplace transforms of some standard functions.
10. Finding the inverse Laplace transform of simple functions.
11. Implementing Laplace transform method of solving ordinary linear differential equations of first and second order with constant coefficient.
12. Finding complementary function and particular integral of constant coefficient second and higher order ordinary differential equations.
13. Finding complementary function and particular integral of constant coefficient second and higher order ordinary differential equations.

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**FIFTH SEMESTER**

**MATHEMATICS V**

**(3 lecture hours per week+ 3 hours of practicals /week per batch of not more than 10 students)**

**THEORY(42 hours)**

**1. ALGEBRA - IV**

**Rings, Integral Domains, Fields**

Rings, Types of Rings properties of rings – Rings of integers modulo  $n$  – Subrings – Ideals ,Principal, Prime and Maximal ideals in a commutative ring – examples and standard properties following the definition – Homomorphism, Isomorphism – Properties – Quotient rings – Integral Domain- Fields - properties following the definition – Fundamental Theorem of Homomorphism of Rings - Every field is an integral domain – Every finite integral domain is a field – Problems.

(14 lecture hours)

## 2. CALCULUS - V

### Differential Calculus Of Scalar And Vector Fields

Scalar field – gradient of a scalar field, geometrical meaning – directional derivative – Maximum directional derivative – Angle between two surfaces - vector field – divergence and curl of a vector field – solenoidal and irrotational fields – scalar and vector potentials – Laplacian of a scalar field – vector identities. Standard properties, Harmonic functions, Problems.

(14 lecture hours)

## 3. NUMERICAL METHODS - I

Finite differences – Definition and properties of  $\Delta, \nabla, \delta, \mu$  and E, the relation between them – The nth differences of a polynomial, Factorial notations, separation of symbols, divided differences and related theorems.

Newton –Gregory forward and backward interpolation formulae – Lagrange's and Newton's interpolation formulae for unequal intervals - Inverse interpolation.

Numerical Integration: Quadrature formula – Trapezoidal rule -Simpon's 1/3 and 3/8 rule(without proofs) and problems.

(14 lecture hours)

### Suggested distribution of lecture hours.

1. Algebra IV: 1 hour /week.
2. Calculus-V (Differential calculus of scalar and vector fields): 1 hours/week
3. Numerical Methods I : 1 hours/week

### Text Books/open source materials

1. Herstein I N, *Topics in Algebra*, 4th ed. New Delhi, India: Vikas Publishing House Pvt. Ltd, 1991.
2. Shanthi Narayan and P K Mittal, *Differential Calculus*, Reprint. New Delhi: S Chand and Co. Pvt. Ltd., 2014.
3. M D Raisinghania, *Vector calculus*, S Chand Co. Pvt. Ltd., 2013.
4. M K Jain, S R K Iyengar, and R K Jain, *Numerical Methods for Scientific and Engineering Computation*, 4th ed. New Delhi, India: New Age International, 2012.
5. [www.scilab.org](http://www.scilab.org).
6. [wxmaxima.sourceforge.net](http://wxmaxima.sourceforge.net)
7. [www.geogebra.org](http://www.geogebra.org)

### Reference Books

1. Michael Artin, *Algebra*, 2nd ed. New Delhi, India: PHI Learning Pvt. Ltd., 2011.

2. Vashista, *A First Course in Modern Algebra*, 11th ed.: Krishna Prakasan Mandir, 1980.
3. John B Fraleigh, *A First course in Abstract Algebra*, 3rd ed.: Narosa Publishing House., 1990.
4. R Balakrishnan and N.Ramabadran, *A Textbook of Modern Algebra*, 1st ed. New Delhi, India: Vikas publishing house pvt. Ltd., 1991.
5. G B Thomas and R L Finney, *Calculus and analytical geometry*, Addison Wesley, 1995.
6. B Spain, *Vector Analysis* , ELBS, 1994.
7. D E Bournes and, P C Kendall, *Vector Analysis*, ELBS, 1996.
8. S S Sastry, *Introductory methods of Numerical Analysis*, Prentice Hall of India, 2012.

#### Useful web links:

1. <http://www.themathpage.com/>
2. <http://www.abstractmath.org/>
3. <http://ocw.mit.edu/courses/mathematics/>
4. <http://planetmath.org/encyclopedia/TopicsOnCalculus.html>
5. <http://ocw.mit.edu/OcwWeb/Mathematics/18-01Fall-2005/CourseHome/index.htm>
6. <http://mathworld.wolfram.com/Calculus.html>
7. <http://www.univie.ac.at/future.media/moe/galerie.html>
8. <http://www.math.gatech.edu/~harrell/calc/>
9. <http://www.amtp.cam.ac.uk/lab/people/sd/lectures/nummeth98/index.htm>
10. <http://math.fullerton.edu/mathews/numerical.html>
11. <http://www.onesmartclick.com/engineering/numerical-methods.html>

### PRACTICALS –V

#### Mathematics practicals with FOSS tools for computer programs (3 hours/ week per batch of not more than 10 students)

#### LIST OF PROBLEMS

1. Examples on different types of rings.
2. Examples on integral domains and fields.
3. Examples on subrings, ideals and subrings which are not ideals.
4. Homomorphism and isomorphism of rings- illustrative examples.
5. To demonstrate the physical interpretation of gradient, divergence and curl.
6. Writing gradient, divergence, curl and Laplacian in cylindrical coordinates.
7. Writing gradient, divergence, curl and Laplacian in spherical coordinates.
8. Using cyclic notations to derive different vector identities.
9. Using cyclic notations to derive some more vector identities.
10. Scilab/Maxima programs on Interpolations with equal intervals.
11. Scilab/Maxima programs on Interpolations with unequal intervals.

12. Scilab/Maxima programs to evaluate integrals using Simpson's  $\frac{1}{3}$ <sup>rd</sup> rule.

13. Scilab/Maxima programs to evaluate integrals using Simpson's  $\frac{3}{8}$ <sup>th</sup> rule.

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## **FIFTH SEMESTER MATHEMATICS – VI**

**(3 lecture hours per week+ 3 hours of practicals/week per batch of not more than 10 students)**

**(42 HOURS)**

### **THEORY**

#### **1. MATHEMATICAL METHODS - II**

##### **Calculus Of Variation**

Variation of a function  $f=f(x, y, y')$  – variation of the corresponding functional – extremal of a functional – variational problem – Euler's equation and its particular forms – Examples – standard problems like geodesics, minimal surface of revolution, hanging chain, Brachistochrone problem –Isoperimetric problems.

(14 Lecture hours)

#### **2. CALCULUS – VI**

##### **a). Line And Multiple Integrals**

Definition of line integral and basic properties examples evaluation of line integrals.

Definition of double integral – its conversion to iterated integrals .Evaluation of double integrals by change of order of integration and by change of variables – computation of plane and surface areas ,volume underneath a surface and volume of revolution using double integrals.

Definition of triple integral and evaluation – change of variables – volume as a triple integral .

(18lecture hours)

##### **b). Integral Theorems**

Green's theorem (with proof) - Direct consequences of the theorem.The Divergence theorem (with proof) - Direct consequences of the theorem.The Stokes' theorem (with proof) - Direct consequences of the theorem.

(10 lecture hours)

### **Suggested distribution of lecture hours**

1. Mathematical Methods II (Calculus of variation): 1 hour /week.
2. Calculus VI (Line and Multiple Integrals and Integral theorems ): 2 hours/week

### **Text Books/open source materials**

1. R Weinstock, *Calculus of Variation*, Dover, 1970.
2. M. D. Raisinghania, *Vector Calculus*, S Chand Co. Pvt. Ltd., 2013.
3. [www.scilab.org](http://www.scilab.org)
4. [wxmaxima.sourceforge.net](http://wxmaxima.sourceforge.net)
5. [www.geogebra.org](http://www.geogebra.org)

### **Reference Books**

1. F B Hildebrand, *Methods in Applied Mathematics*,
2. B Spain, *Vector Analysis* , ELBS, 1994.
3. D E Bournesand, P C Kendall, *Vector Analysis*, ELBS, 1996.

### **Useful web links:**

1. <http://ocw.mit.edu/courses/mathematics/>
2. <http://planetmath.org/encyclopedia/TopicsOnCalculus.html>
3. <http://mathworld.wolfram.com/Calculus.html>
4. <http://www.univie.ac.at/future.media/moe/galerie.html>
5. <http://www.math.gatech.edu/~harrell/calc/>

## **PRACTICALS –VI**

**Mathematics practicals with FOSS tools for computer programs  
( 3 hours/ week per batch of not more than 10 students)**

### **LIST OF PROBLEMS**

1. Example on Euler's equation in full form.
2. Example on particular forms of Euler's equation.
3. Examples on minimum surface of revolution and Brachistochrone problem.
4. Examples on Isoperimetric problems.
5. Evaluation of the line integral with constant limits.
6. Evaluation of the double integral with constant limits.
7. Evaluation of the triple integral with constant limits.
8. Evaluation of the line integral with variable limits.
9. Evaluation of the double integral with variable limits.
10. Evaluation of the triple integral with variable limits.
11. Verifying Green's theorem.
12. Verifying Gauss divergence theorem.
13. Verifying Stokes' theorem

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## **SIXTH SEMESTER MATHEMATICS - VII**

**(3 lecture hours per week+ 3 hours of practicals /week per batch of not more than 10 students)**

**(42 HOURS)**

### **THEORY**

#### **1. ALGEBRA –V**

##### **Linear Algebra**

Vector space – Examples – Properties – Subspaces – criterion for a subset to be a subspace –linear span of a set - linear combination – linear independent and dependent subsets – Basis and dimensions– Standard properties – Examples illustrating concepts and results.

Linear transformations – properties – matrix of a linear transformation – change of basis – range and kernel – rank and nullity – Rank – Nullity theorem – Non-singular and singular linear transformations - Standard properties – Examples.

(14 lecture hours)

#### **2. DIFFERENTIAL EQUATIONS III**

##### **a). Orthogonal Curvilinear Coordinates**

Definition of orthogonal curvilinear coordinates. Fundamental vectors or base vectors, Scale factors or material factors - quadratic differential form. Spherical curvilinear system : Cartesian, Cylindrical – conversion of Cylindrical to orthogonal Spherical polar coordinates. Theorem: The Spherical coordinate system is orthogonal curvilinear coordinate system. (without proof) No problems on conversions of one system to another.

##### **b). Partial Differential Equations**

Total differential equations-Necessary condition for the equation  $Pdx+ Qdy+Rdz=0$  to be integrable-Simultaneous equations of the form  $\frac{dx}{P} = \frac{dy}{Q} = \frac{dz}{R}$

Formation of partial differential equation .Equations of First Order Lagrange's linear equation – Charpit's method, Standard types of first order non-linear partial differential equation (By known substitution).

Solution of second order linear partial differential equations in two variables with constant coefficients by finding complementary function and particular integral

Solution of one – dimensional heat equations, Solution of one – dimensional wave equations using Fourier series.

(28 lecture hours)

### **Suggested distribution of lecture hours:**

1. Algebra-V (Linear Algebra) : 1 hours / week.
2. Differential Equations III: 2 hours / week

### **Text Books/open source materials**

1. Krishnamoorthy V K and Mainra V P and Arora J L, *An Introduction to Linear Algebra*, Reprint. New Delhi, India: Affiliated East West Press Pvt. Ltd., 2003.
2. M. D. Raisinghania, *Vector Calculus*, S Chand Co. Pvt. Ltd., 2013.
3. M D Raisinghania, *Ordinary and Partial Differential Equations*, S Chand and Co. Pvt. Ltd., 2014.
4. [www.scilab.org](http://www.scilab.org)
5. [wxmaxima.sourceforge.net](http://wxmaxima.sourceforge.net)
6. [www.geogebra.org](http://www.geogebra.org)

### **Reference Books**

1. G Strang, MIT open courseware (<http://ocw.mit.edu/courses>).
2. B Spain, *Vector Analysis*, ELBS, 1994.
3. D E Bournes and, P C Kendall, *Vector Analysis*, ELBS, 1996.
4. Frank Ayres, *Schaum's outline of theory and problems of Differential Equations*, 1st ed. USA: McGraw-Hill, 1972.
5. GF Simmons, *Differential equation with Applications and historical notes*, 2nd ed.: McGraw-Hill Publishing Company, Oct 1991.
6. S Narayanan & T K Manicavachogam Pillay, *Differential Equations.*: S V Publishers Private Ltd., 1981.
7. I N Sneddon, *Elements of Partial Differential Equations*, 3rd ed.: Mc. Graw Hill., 1980.

### **Useful web links:**

1. <http://ocw.mit.edu/courses/mathematics/>
2. <http://mathworld.wolfram.com/Calculus.html>
3. <http://www.math.gatech.edu/~harrell/calc/>
4. <http://tutorial.math.lamar.edu/classes/de/de.aspx>
5. <http://www.sosmath.com/diffeq/diffeq.html>
6. [http://www.analyzemath.com/calculus/Differential\\_Equations/applications.html](http://www.analyzemath.com/calculus/Differential_Equations/applications.html)

## **PRACTICALS –VII**

### **Mathematics practicals with FOSS tools for computer programs (3 hours/ week per batch of not more than 10 students)**

### **LIST OF PROBLEMS**

1. i. Vector space, subspace – illustrative examples.  
ii. Expressing a vector as a linear combination of given set of vectors.  
iii. Examples on linear dependence and independence of vectors.
2. i. Basis and Dimension – illustrative examples.  
ii. Verifying whether a given transformation is linear.

3. i. Finding matrix of a linear transformation.  
ii. Problems on rank and nullity.
4. Plotting of cylinder and cone using orthogonal curvilinear coordinates.
5. Plotting of sphere using orthogonal curvilinear coordinates.
6. Solutions to the problems on total and simultaneous differential equations.
7. Solutions to the problems on different types of Partial differential equations.
8. Solving second order linear partial differential equations in two variables with constant coefficient.
9. Solving some more second order linear partial differential equations in two variables with constant coefficient.
10. Solution of one dimensional heat equation using Fourier series with Dirichlet condition.
11. Solution of one dimensional heat equation using Fourier series with Neumann condition.
12. Solution of one dimensional wave equation using Fourier series with Dirichlet condition.
13. Solution of one dimensional wave equation using Fourier series with Neumann condition.

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## **SIXTH SEMESTER MATHEMATICS - VIII**

**(3 lecture hours per week+ 3 hours of practicals /week per batch of not more than 10 students)**

**(42 HOURS)**

### **THEORY**

#### **1. ANALYSIS - III**

##### **Complex Analysis**

Complex numbers-Cartesian and polar form-geometrical representation-complex-Plane-Euler's formula-  $e^{i\theta} = \cos \theta + i \sin \theta$ . Functions of a complex variable-limit, continuity and differentiability of a complex function. Analytic function Cauchy-Riemann equations in Cartesian and Polar forms-Sufficiency conditions for analyticity(Cartesian form only)-Harmonic function-standard properties of analytic functions-construction of analytic function when real or imaginary part is given-Milne Thomson method.

Complex integration-the complex integration –properties-problems.Cauchy's Integral theorem-proof using Green's theorem- direct consequences.Cauchy's Integral formula with proof-Cauchy's generalised formula for the derivatives with proof and

applications for evaluation of simple line integrals - Cauchy's inequality with proof – Liouville's theorem with proof. Fundamental theorem of algebra with proof.

Transformations – conformal transformation – some elementary transformations namely Translation, rotation, magnification and inversion - examples.

The bilinear transformation (B.T.)-cross ratio-invariant points of a B.T.-properties-

- (i) B.T. sets up a one to one correspondence between the extended  $z$ -plane and the extended  $w$ -plane.
- (ii) Preservation of cross ratio under a B.T.
- (iii) A B.T. transforms circles onto circles or straight lines.

Problems on finding a B.T., and finding images under a B.T. and invariant points of a B.T. Discussion of transformations  $w = z^2$ ,  $w = \sin z$ ,  $w = \cosh z$  and  $w = e^z$ .

(28 lecture hours)

## 2. NUMERICAL METHODS – II

Numerical solutions of algebraic and Transcendental equations – method of successive bisection - method of false position – Newton-Raphson method. Numerical solutions of non-Homogeneous system of linear algebraic equations in three variables by Jacobi's method and Gauss-Seidel method. Computation of largest Eigen value of a square matrix by power method.

Solutions of initial value problems for ordinary linear first order differential equations by Taylor's series, Euler's and Euler's modified method and Runge-Kutta 4<sup>th</sup> ordered method.

(14 lecture hours)

### **Suggested distribution of lecture hours:**

1. Analysis-III (Complex Analysis): 2 hours / week.
2. Numerical Methods-II: 1 hour / week

### **Text Books/open source materials**

1. S Shanthinarayan, *Complex Analysis*, S Chand Co. Pvt. Ltd., 2012.
2. M K Jain, S R K Iyengar, and R K Jain, *Numerical Methods for Scientific and Engineering Computation*, 4th ed. New Delhi, India: New Age International, 2012.
3. [www.scilab.org](http://www.scilab.org)
4. [wxmaxima.sourceforge.net](http://wxmaxima.sourceforge.net)
5. [www.geogebra.org](http://www.geogebra.org)

### **Reference Books**

1. R V Churchill & J W Brown, *Complex Variables and Applications*, 5th ed.: McGraw Hill Companies., 1989.
2. L V Ahlfors, *Complex Analysis*, 3rd ed.: Mc Graw Hill. , 1979.
3. A R Vashista, *Complex Analysis*, Krishna Prakashana Mandir, 2012.
4. S S Sastry, *Introductory methods of Numerical Analysis*, Prentice Hall of India, 2012.

**Useful web links:**

1. <http://www.mathcs.org/analysis/real/index.html>
2. <http://www.amtp.cam.ac.uk/lab/people/sd/lectures/nummeth98/index.htm>
3. <http://math.fullerton.edu/mathews/numerical.html>
4. <http://www.onesmartclick.com/engineering/numerical-methods.html>

**PRACTICALS –VIII****Mathematics practicals with FOSS tools for computer programs  
(3 hours/ week per batch of not more than 10 students)****LIST OF PROBLEMS**

1. Some problems on Cauchy-Riemann equations (polar form).
2. Implementation of Milne-Thomson method of constructing analytic functions (simple examples).
3. Illustrating orthogonality of the surfaces obtained from the real and imaginary parts of an analytic function.
4. Verifying real and imaginary parts of an analytic function being harmonic (in polar coordinates).
5. Illustrating the angle preserving property in a transformation.
6. Illustrating that circles are transformed to circles by a bilinear transformation.
7. Examples connected with Cauchy's integral theorem.
8. Solving algebraic equation (Bisection method).
9. Solving algebraic equation (Regula-Falsi and Newton-Raphson methods).
10. Solving system of equations (Jacobi and Gauss-Seidel methods).
11. Solving for largest eigenvalue by Power method.
12. Solving ordinary differential equation by modified Euler's method.
13. Solving ordinary differential equation by Runge-Kutta method of 4<sup>th</sup> order.

**Note:** The above list may be changed annually with the approval of the BOS in UG (Mathematics). Geogebra/Octave may also be used in place of scilab/maxima.